Dispersion Anisotropy of Plasmon–Exciton–Polaritons in Lattices of Metallic Nanoparticles

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ABSTRACT: When the electromagnetic modes supported by plasmonic-based cavities interact strongly with molecules located within the cavity, new hybrid states known as plasmon–exciton–polaritons (PEPs) are formed. The properties of PEPs, such as group velocity, effective mass, and lifetime, depend on the dispersive and spectral characteristics of the optical modes underlying the strong coupling. In this work, we focus on lattice modes supported by rectangular arrays of plasmonic nanoparticles known as surface lattice resonances (SLRs). We show that SLRs arising from different in-plane diffraction orders in the lattice can couple with the molecular excitons, leading to PEPs with distinct dispersions and thus different group velocities. These results illustrate the possibility of tailoring the transport of PEPs through the design of lattices of plasmonic particles.

KEYWORDS: strong coupling, exciton–polaritons, plasmonics lattice, organic fluorophores, anisotropic dispersions

The realization of strong light–matter coupling at room temperature using organic molecules to exploit properties of exciton–polaritons has been the driving force of many theoretical and experimental studies in recent years. Exciton–polaritons possess intriguing properties that have been exploited for wide-ranging purposes: room-temperature Bose–Einstein condensation and polariton lasing,1–4 enhanced exciton transport,5–8 and conductivity in organic semiconductors, modified electronic potential energy surfaces in molecular systems,9,10 and altered chemical reaction yields10,11 constitute a small set of associated research highlights across numerous disciplines.

In the realm of strong light–matter coupling, microcavities have historically been the canonical system for studying exciton–polaritons12 by virtue of their intuitive design and robust cavity modes. In recent room-temperature experiments the types of photonic structures employed for strong coupling have the multiplied, ranging from single plasmonic nanoparticles to planar metallic surfaces,13,14 plasmonic hole arrays,15 and nanoparticle arrays.16,17,18 The hybrid quasi-particles resulting from the strong coupling of molecular excitons with modes in plasmonic resonances, i.e., modes arising from the coherent oscillation of the electrons at the interface between the metal and the surrounding dielectric, are called plasmon–exciton–polaritons (PEPs).

The strength of microcavities lies in the high-quality resonances associated with their well-defined cavity modes. Plasmonic structures, on the other hand, suffer from strong radiative and nonradiative losses,19 resulting in relatively broad line widths. The improvement of the resonance quality factor leads to increased lifetimes, a condition that makes the realization of strongly coupled coherent states feasible. Nevertheless, the strong field enhancement within a small mode volume at the vicinity of these structures has made the realization of strong light–matter coupling possible.20

Among the aforementioned plasmonic structures, it has been shown that periodic arrays of plasmonic nanoparticles are suitable platforms for strong coupling experiments.4,17,18,21–23 Plasmonic arrays offer the dual advantage of independent control over both the energy-momentum dispersions and the line widths of collective resonances (surface lattice resonances, SLRs) supported by the arrays.24 The modification of the dispersion is of central relevance for the design of photonic systems enabling the precise control of the properties of the exciton–polaritons, including group velocity and effective mass.17 Furthermore, these systems benefit from an ease in positioning the organic molecules in the vicinity of the plasmonic nanoparticles25 and the possibility for integration.

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with planar photonic technologies due to the open nature of the cavity.

In this article, we demonstrate strong coupling of excitons in organic molecules to SLRs in anisotropic arrays of nanoparticles. By exploiting the coupling of excitons to different orders of diffraction, we allow for the excitation of PEPs with different dispersions and group velocities. This leads to an anisotropy in the properties of the generated PEPs which can not take place in a conventional cavity, where cylindrical symmetry limits the dispersion. By combining PEP dispersions with different propagation constants in different directions, it is conceivable to design systems analogous to birefringent crystals for nonlinear polaritons or provide directivity in the transport and propagation of exciton—polaritons for optoelectronic applications.

**SAMPLE PREPARATION**

Arrays of nanoparticles were fabricated by substrate conformal imprint lithography onto glass substrates (Corning Eagle 2000, $n = 1.51$). This technique, which is based on a polydimethylsiloxane (PDMS) stamp to conformally imprint nanostructures, offers a great potential for fabrication of nanostructures over large areas with high precision and reproducibility. In this study, we used silver as a metal with low loss in the visible range. To avoid this oxidation, the oxidation under ambient conditions, which can deteriorate their optical and plasmonic responses. To strongly couple the molecular excitons to the SLRs supported by the array, a layer of poly(methyl methacrylate) (PMMA) containing the molecules with thicknesses of $120 \pm 20$ nm was spin-coated on top of the array. Small variations of the thickness within the error range does not influence the optical properties of SLRs. We dissolved the dye molecules and PMMA in chloroform and stirred the solution at $60^\circ$C for 1 h. Two different samples were prepared with a weight concentration of the organic molecules with respect to PMMA of 35 and 50 wt %.

**SURFACE LATTICE RESONANCES IN ARRAYS OF NANOPARTICLES**

To have a better insight into the electric field distribution of the resonances supported by the metallic nanoparticles, we have performed finite-difference time-domain (FDTD) simulations for the single particle as well as for an array of nanoparticles with the lattice parameters described above. In all the simulations, the structure is illuminated at normal incidence with a plane wave with the polarization vector oriented along the short axis of the nanoparticles. In Figure 2(a), the scattering cross section of the single particle with a resonance at $E_{\text{LSPR}} = 2.5$ eV is plotted with a red curve. This resonance corresponds to the localized surface plasmon resonance (LSPR) with a dipolar ($\lambda/2$) electric field distribution. The total electric field intensities corresponding to the LSPR for the plane across the middle of the particle (top view) and the cross sectional plane (side view) are shown in Figure 2(b,c) in a logarithmic scale. The LSPR creates a strong electric enhancement at the vicinity of the nanoparticles. However, the extension of the field to the surrounding medium is limited to few tens of nanometers. This spatial confinement reduces the efficient coupling of the electromagnetic field to a few of the molecules distributed in the PMMA layer. Furthermore, the strong ohmic and radiative losses associated with LSPRs lead to the broad line width and short lifetime of these resonances.

The losses associated with LSPRs in individual particles can be significantly reduced by creating a lattice of plasmonic nanoparticles in which the particles interact via coherent scattering by means of the in-plane diffraction orders, known as Rayleigh anomalies (RAs). The RAs lead to the enhanced radiative coupling between LSPRs, resulting in a remarkable modification of the line width and quality factor of the resonance. The resulting modes are the aforementioned SLRs. In this case, the electric field on each particle is the sum of the incident field plus the radiation from all other nanoparticles. The effective polarizability of each nanoparticle in an infinite array is given by

$$\alpha^* = \frac{1}{1/\alpha - S}$$

where $\alpha$ is the polarizability of the single particle and $S$ is the retarded dipole sum, which contains the effect of all the other nanoparticles on the polarizability. The extinction cross section

![Figure 1](image-url)
of the array of coupled particles in terms of effective polarizability can be written as

$$C_{\text{ext}} = 4\pi k \text{Im}(\alpha^*)$$  \hspace{1cm} (2)

The simulated extinction of the array supporting the enhanced diffractive coupling between LSPRs is shown in Figure 2(a) as a blue curve. The extinction is defined as \((1 - T/T_{\text{ref}})\) where \(T\) is the zeroth-order transmission, i.e., transmission in the forward direction from the array, and \(T_{\text{ref}}\) is the transmission from the sample in the absence of the nanoparticles, i.e., the transmission of the substrate. The appearance of a narrow peak in the extinction of the periodic array of nanoparticles can be explained in terms of interplay between S and \(1/\alpha\). The measured extinction at normal incidence is displayed in Figure 2(a) as a gray line. The measurement is shifted vertically for clarity, and it shows a good agreement with the simulations. The small discrepancies between the simulated and measured extinction spectra can be explained by the Gaussian beam illumination and finite sample size in the experiment, compared to the plane wave illumination and infinite sample size for the simulations. Moreover, small size variations between the simulated and measured nanoparticles could also induce some discrepancies.

A significant reduction of the line width (enhanced quality factor) is observed for the array of nanoparticles. Moreover, due to the photonic nature of the diffraction order giving rise to the SLRs, these modes exhibit a more spatially extended electric field profile than LSPRs. Given the fact that the lattice is formed by plasmonic nanoparticles with large polarizability, the local electric field intensity of the modes is enhanced due to LSPRs. This effect can be revealed through the comparison between the spatial distribution of electric field intensity for a single nanoparticle (Figure 2(b,c)) and the nanoparticle in the lattice (Figure 2(d,e)). In Figure 2(d,e), we can see the simultaneous delocalization and enhancement of the electric field intensity in the lattice. The spatial modification of the electromagnetic field and its further extension into the regions far from the particle lead to an increase in the number of molecules that can couple to the electromagnetic mode, resulting in an increased collective coupling strength of the molecular excitons with the SLRs.

\section*{STRONG COUPLING OF EXCITONS TO SLRS}

One of the signatures of strong light–matter coupling is the modification of the energy dispersion and the appearance of an anticrossing at the energy and momentum where the dispersions of the lattice modes and molecular excitonic transition cross each other. To measure the strong coupling between the molecular excitons and the SLRs, we have implemented angle-resolved measurements in order to measure the optical extinction as a function of the angle of incidence, i.e., as a function of the wave vector parallel to the surface of the array. These measurements retrieve the dispersive behavior of the resonances supported by the array. The collective nature of the strong coupling implies that the strength of the light–matter interaction should increase by increasing the number of the excitons within the mode volume of the cavity, leading to an enhanced anticrossing in the dispersion. The coupling strength in the collective strong coupling is given by the Rabi energy:

$$\hbar \Omega = 2\bar{E} \bar{d} \sqrt{N}$$  \hspace{1cm} (3)

where \(\bar{E}\) and \(\bar{d}\) are the electromagnetic field amplitude and the transition dipole moment of the exciton, respectively, and \(N\) is the number of excitons coupled to the optical mode that expresses the collective nature of strong coupling.\(^{29}\)

To strongly couple SLRs to molecular excitons, we spin-coated a layer of PMMA doped with the dye molecules at 35 and 50 wt %. In these experiments we select the periodicity of the lattice such that the energy of the SLRs at zero momentum,
Figure 3. Measurements of the extinction for the array of nanoparticles with SLR excited along the (0, ±1) RAs while the array is covered with 120 nm (a, d) of undoped PMMA and doped PMMA with (b, e) 35 wt % and (c, f) 50 wt % dye. (a–c) SLR and PEP dispersions when excited along the x-direction. (d–f) SLR and PEP dispersions along the y-direction. Black dashed lines indicate the excitonic and vibronic transition of the dye.

The SLRs with linear dispersions are displayed in Figure 3(d). Similar to the previous case, the strong coupling of the SLRs with the molecular excitons, shown in Figure 3(e) and (f) for 35 and 50 wt % dye concentration, respectively, leads to their hybridization and the formation of PEPs with an anticrossing at \( k_y \approx 1.5 \text{ mrad/nm} \). As we show ahead, one important result of this simultaneous occurrence of PEPs with

\[ E_{(0, \pm 1)} = \pm \frac{\hbar c}{n_{\text{eff}}} \sqrt{k_x^2 + (2\pi/a_y)^2} \]  

where \( a_y = 380 \text{ nm} \) and \( \vec{k}_{\parallel} = k_y \hat{u}_y \) has only a component along the x-direction; that is, the sample is rotated along the y-direction. The measured full width at half-maximum (fwhm) of this SLR is 16 meV at \( k_x = 0 \text{ mrad/nm} \). The fwhm of the SLR increases by increasing \( k_x \) due to the reduction of the detuning between the RAs and the LSPR (at \( E = 2.458 \text{ eV} \)), which results in an enhanced plasmonic character of the SLR. Moreover, one should notice that the dispersion of the SLR along \( k_x \) and \( k_y \) is quite different, a difference that also extends to the line widths. For this particular system, it seems that the SLR along \( k_y \) is more damped than along \( k_x \). As the resonances in these systems have Fano lineshapes, one can also describe the features of the resonance such as line width by the strength of the coupling between the discrete state (RAs) and the continuum (LSPRs), which depends on the dispersion of the RAs. The SLRs with linear dispersions are displayed in Figure 3(d). Similar to the previous case, the strong coupling of the SLRs with the molecular excitons, shown in Figure 3(e) and (f) for 35 and 50 wt % dye concentration, respectively, leads to their hybridization and the formation of PEPs with an anticrossing at \( k_y \approx 1.5 \text{ mrad/nm} \). As we show ahead, one important result of this simultaneous occurrence of PEPs with
distinct dispersion anisotropy is the modified PEP group velocity. An interesting feature that can be seen in the dispersion of the strongly coupled linear SLRs to excitons is the dark nature (absence of extinction) of the upper polariton band at $k_y = 0$ mrad/nm. A similar response has been reported previously, and it is explained by the antisymmetric field and charge distributions across the nanoparticles due to the optical retardation along their long axis. These distributions lead to the suppression of the net dipole moment and the absence of extinction. Recent experiments showing exciton–polariton lasing in nanoparticle arrays have revealed the relevance of dark modes for PEP condensation. We note also that the SLRs associated with the $(\pm 1, 0)$ RAs are not visible in the extinction measurements of Figure 3. This absence is due to the shorter lattice constant along the $x$-direction ($a_x = 200$ nm), which shifts these resonances to higher frequencies.

To determine the coupling strength and group velocities of PEPs along different directions, we can fit the measurements to a few-level Hamiltonian given by

$$
H = \begin{pmatrix}
E_{\text{SLR}} & \hbar \Omega_1 & \hbar \Omega_2 \\
\hbar \Omega_1 & E_{X1} & 0 \\
\hbar \Omega_2 & 0 & E_{X2}
\end{pmatrix}
$$

(7)

where $E_{\text{SLR}}$ is the energy of the SLR and $E_{X1}$ and $E_{X2}$ are the energies of the vibronic bands. Here, we focus on the linear-response regime, such that the two dominant vibronic peaks can be treated as separate independent resonances of the molecule. Moreover, $\hbar \Omega_1$ and $\hbar \Omega_2$ are the Rabi energies describing the coupling between the SLR and the molecular transitions. Note that in this model we treat the different SLRs independently from each other. By diagonalizing this Hamiltonian, we can obtain the energy eigenvalues of the system. In Figure 4(a,b), the green solid lines correspond to the fitted dispersions to the measured lower PEP bands for the sample with 50 wt % dye concentration. The red dots in these figures represent the experimental values obtained from the measurements of Figure 3(c,f). A good agreement between the measured and calculated dispersions is achieved. However, there are some discrepancies that can be related to the simplified nature of the model and the fact that it does not take into account all the molecular energy sublevels and transitions that can also couple to the SLRs. In addition, in the energy region where the upper polariton modes are expected, there are a number of additional photonic modes in the system (e.g., guided modes in the polymer layer). As we have not included these modes in the simple model we use to obtain the lower polariton dispersion, the middle and upper polaritons of the model Hamiltonian do not correspond well to the actual modes of the system. Therefore, we do not discuss their dispersions in detail.

Figure 4. Dispersions of the lower polaritons (red dots) obtained from the extinction maps for SLRs propagating along the (a) $y$- and (b) $x$-direction. The solid green and yellow lines represent the polaritons resulting from the analytical model based on the described Hamiltonian. The black dashed line at $E_{X1} = 2.24$ eV ($E_{X2} = 2.41$ eV) represents the energy of the excitonic (vibronic) transition in the molecules. The blue dashed line represents the energy dispersion of SLRs in the absence of dye molecules.

Figure 5. (a) Three-dimensional dispersion of PEPs. The color indicates the photon fraction of the PEPs. The photon fraction of $\sim 0.5$ around the Rabi splitting indicates the strong plasmonic behavior of the exciton–polaritons. (b) Group velocity of PEPs as a function of $k_x$ (blue circles) and $k_y$ (red circles).
Using these fits we extract the value of ~120 meV for the Rabi energy of the (0, ±1) PEPs with 35 wt % dye concentration, which is greater than the line widths of SLRs (77 meV) and the inhomogeneously broadened excitonic transition (90 meV). By increasing the dye concentration to 50 wt % we observe that the Rabi splitting increases to ~170 meV for PEPs along k_x and k_y.

To emphasize the anisotropy on the dispersion of the PEPs, we have reconstructed the three-dimensional PEP dispersion in Figure 5(a). The dispersions are extracted from the diagonalization of the few-level Hamiltonian given by eq 7. The photon fraction of the PEPs is color-coded in Figure 5(a).

A close look into this figure shows that the curvature of the dispersion surfaces is different along different directions. In comparison with microcavities that manifest cylindrical symmetry and isotropic dispersion, arrays of nanoparticles can have very anisotropic dispersion. One immediate consequence of this anisotropic dispersion is the different group velocity along k_x and k_y, while the blue curve shows the group velocity along k_x. The anisotropic nature of the PEPs will also enable controlling the scattering of the exciton–polaritons applicable for exciton–polariton condensation and parametric oscillation and amplification.

In order to determine the PEPs’ group velocities along the x and y directions, we have calculated the first derivative of the dispersion from the experimental extinction maxima. The group velocities of the PEPs, normalized by the speed to light in a vacuum, are shown in Figure 5(b) as a function of the wave vector. In this figure, the red curve corresponds to the group velocity of the lower PEP band along k_y, while the blue curve shows the group velocity along k_x. The anisotropy in the dispersion leads to very different group velocities, with a velocity ratio close to 10 for small values of the wave vector. While the close-to-linear dispersion for k_x leads to a large group velocity, the parabolic dispersion for k_y leads to slow PEPs. In addition to the different dispersions along different directions, the difference in the curvature of the PEPs should lead to distinct effective masses and anisotropic transport of exciton–polaritons. For SLRs arising from the diffraction along x-direction, the effective mass can be calculated from the second derivative of the dispersion \(m^* = 4 \times 10^{-4}m_e\) at \(k = 0\ mrad/\nm\), where \(m_e\) is the electron mass.

For SRLs along the y-direction, the dispersions are linear and the effective mass of the relativistic particles needs to be taken into account.

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**CONCLUSION**

In conclusion, we have shown that planar arrays of metallic nanoparticles can provide a powerful platform for creating the hybrid states of light and matter, plasmon–exciton–polaritons, with distinct dispersions and enable making a polaritonic medium with tailored anisotropy. The quality of the fabricated arrays and their associated geometrical parameters lead to the observation of Rabi splitting between the upper and lower PEPs with different polariton dispersions and group velocities. Such degree of control of the properties of PEPs can be potentially applicable for the design of polariton-based circuits with an anisotropic response.


