Dynamics of the Formation and Decay of Coherence in a Polariton Condensate

E. del Valle,[1] D. Sanvitto,[2] A. Amo,[2,*] F. P. Laussy,[1] R. André,[3] C. Tejedor,[4] and L. Viña[2]

[1]*School of Physics and Astronomy, University of Southampton, SO171BJ, Southampton, United Kingdom*
[2]*Departamento Física de Materiales, Universidad Autónoma de Madrid, 28049, Madrid, Spain*
[3]*CEA-CNRS, Institut NEEL-CNRS, B.P. 166, 38042 Grenoble Cedex 9, France*
[4]*Departamento Física Teórica de la Materia Condensada, Universidad Autónoma de Madrid, 28049, Madrid, Spain*

We study the dynamics of the formation and decay of a condensate of microcavity polaritons. We investigate the relationship among the number of particles, the emission linewidth, and its degree of linear polarization, which serves as the order parameter. Tracking the condensate formation, we show that coherence is not determined only by occupation of the ground state, bringing new insights into the determining factors for Bose-Einstein condensation.

Whereas a lot is known of the thermodynamics of quantum fluids—at equilibrium and in infinite size systems—the dynamics of formation of a Bose-Einstein condensate (BEC) is still vastly an open question. This dynamics is not easily detectable in atomic BECs and has not been studied experimentally, due to the very short time scale in which cold atomic gases reach thermal equilibrium. A good alternative to investigate the process of condensate formation is that of microcavity polaritons [1], although this system differs from atomic condensates due to its intrinsically out-of-equilibrium character. Polaritons arise from the strong coupling of photons and excitons in semiconductor microcavities [2] and have recently been shown to undergo a nonequilibrium phase transition with a spontaneous buildup of coherence in the ground state [3–7], similar to what has been observed in atomic BECs [8,9]. Thanks to the small polariton lifetime, various properties can be tracked continuously from the photons they emit. This has been used to measure the spatial first order coherence [10], the temporal first and second order correlation functions [11,12] and even real time dynamics such as propagation [13].

The dynamical evolution and origin of the degree of coherence in a polariton condensate remain however unclear. Intriguing results have been recently reported of 1 order of magnitude increase of the ground-state polariton coherence time, by reducing particle fluctuations in the excited states [12]. Such experiments reveal the possibilities for the dynamical observation of condensation [14]. Also, some theoretical studies have been reported based on stochastic simulations of the order parameter [15]. In this work, we pursue this goal both experimentally and theoretically and track the dynamics of the formation of a polariton BEC, following how the condensation forms and decays in a pulsed experiment.

Since polaritons have a spin degree of freedom that is passed to the polarization of the photon they emit, the buildup of off-diagonal elements in the density matrix (characteristic of coherent states) can be accessed through the degree of linear polarization:

$$D_l = 2 \, | \, \Re \langle a_{0\uparrow} a_{0\downarrow}^\dagger \rangle \, | \, / (\langle a_{0\uparrow}^\dagger a_{0\uparrow} \rangle + \langle a_{0\downarrow}^\dagger a_{0\downarrow} \rangle), \qquad (1)$$

with $a_{0\uparrow}$ and $a_{0\downarrow}$ the field operators for spin-up (right-circular polarization) and spin-down (left-circular polarization) polaritons, respectively. If spin-up and spin-down polaritons are uncorrelated, with a thermal distribution and no determined phase relationship, the light is unpolarized. If, however, the two spin projections are condensed with well defined order parameters $\langle a_{0\uparrow} \rangle$ and $\langle a_{0\downarrow} \rangle$ that factorize the numerator of Eq. (1), the emitted light acquires a definite polarization. Therefore, D_l is linked to the degree of coherence of the condensate and to the imbalance between spin-up and spin-down polariton populations [6,11,16,17]. The spin degeneracy can be lifted, producing a Zeeman splitting of polariton energies. If we further assume that the two spin populations have similar evolutions, these can be modeled with a convolution of thermal and coherent states [16,18] with time-dependent thermal and coherent fractions. In our case, we have observed experimentally that, except for a short transient after the pulsed excitation, spin-up and spin-down populations equalize and evolve similarly in time [19]. Therefore the degree of linear polarization is directly related to the degree of second order coherence (at zero delay) $g^{(2)}$ of the polariton gas: $D_l \approx \sqrt{2 - g^{(2)}}$. If the spin populations have very different dynamics, one has to keep track of the coherence degree of each of the two spin components, and this simple expression no longer holds. Up to now, this relationship has been exploited for measuring the degree of coherence only in stationary situations [6,11]. In this work, we use it to study experimentally the dynamics of condensation. Using simultaneous detection of energy- and time-resolved photoluminescence, together with the degree of linear polarization of the ground state, we monitor the formation and decay of the polariton condensate in the ground state after a circularly polarized, pulsed excitation at high energy. Comparing our data with a phenomeno-

logical model, we investigate the evolution of the conden-
sate statistics and coherence.

In the experiments, polaritons are created in a CdTe-
based microcavity grown by molecular beam epitaxy. The
sample consists of a $Cd_{0.4}Mg_{0.6}Te$ 2λ cavity with top
(bottom) distributed Bragg reflectors of 17.5 (23) pairs of
alternating $\lambda/4$-thick layers of $Cd_{0.4}Mg_{0.6}Te$ and
$Cd_{0.75}Mn_{0.25}Te$. Four CdTe quantum wells of 50 Å thick-
ness, separated by a 60 Å barrier of $Cd_{0.4}Mg_{0.6}Te$, are
placed in each of the antinodes of the electromagnetic
field. Exciton-photon coupling is achieved with a Rabi
splitting of 23 meV; the sample is kept at 4 K, and con-
densation is obtained around zero detuning between the
exciton and the bare cavity dispersion. Photons are injected
via circularly polarized, picosecond-long pulses tuned at
the first minimum above the Bragg mirror stop band
(~40 meV from the bottom of the dispersion) in order to
guarantee the memory loss of the laser polarization and the
coherence by the time polaritons are formed at the bottom
of the band. Light escaping from the microcavity is dis-
persed through a 0.5 m spectrometer and analyzed with a
streak camera. This allows one to resolve in time the
intensity and energy of the emission of the ground state
[Figs. 1(a) and 1(b)] and simultaneously analyze the direc-
tion and linear degree of polarization of the emitted light
together with the polariton linewidth [Fig. 1(c) and insets].
The direction of the linear polarization is pinned to a
crystallographic axis, as has been observed with continu-
ous pumping in a sample of the same batch growth [11] and
with pulsed pumping in samples similar to ours [20].
Without this pinning, the polarization would average to
zero, which is detrimental to our approach but is otherwise
one of the most direct demonstrations of symmetry break-
ing associated to the quantum phase transition, as reported
in Ref. [6]. In our case, the direction of the pinning depends
on the point of the sample, as shown in the insets (I) and
(II) in Fig. 1(c).

The nonresonant excitation creates a large population of
carriers, at high energies, that form the polaritons. Thanks
to the quick relaxation mechanisms, such as phonon emis-
sion and polariton-polariton scattering [21], the population
of polaritons relaxes into the fundamental state (with in-
plane momentum $k = 0$). Figure 1 depicts the experimen-
tal time evolution of the ground state after the arrival of the
pulse at some time $t < 0$, until the complete decay of the
condensate. The intensity of the light emitted by the con-
densate, first shown in Fig. 1(a), right (in density plot), is
normalized to represent the ground-state population n_0 in
Fig. 1(c) (blue circles). The abrupt change into a nonlinear
growth—associated with the onset of stimulated enhance-
ment—is matched to 1. We note from the ground-state en-
ergy [Fig. 1(a)] that the dispersion is already blueshifted
(as compared to the long time energy, at $t \gtrsim 300$ ps), even
when n_0 is very small (at $t \simeq 0$). This confirms that the
blueshift is mainly due to exciton screening and carrier-
carrier interaction in the exciton reservoir [22–24] and
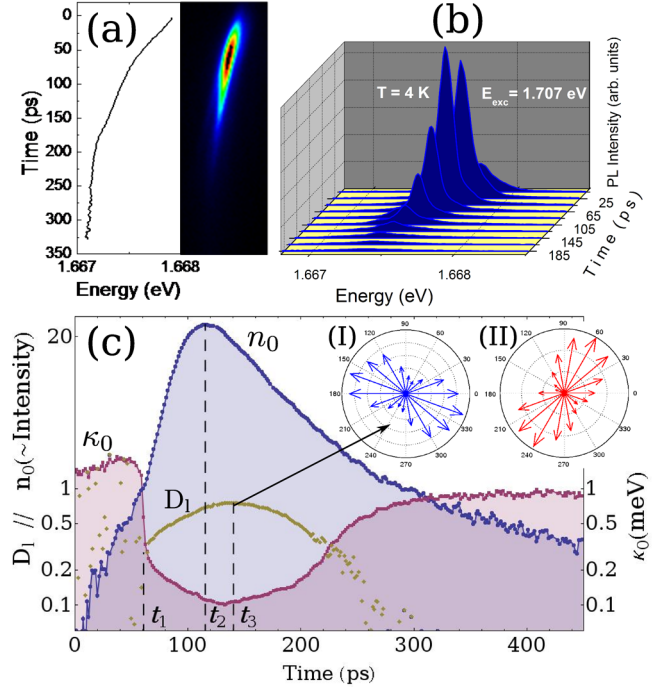that it is only slightly affected by the ground-state occu-

FIG. 1 (color online). Experimental results on the dynamics of
BEC formation after the arrival of the nonresonant pulse.
(a) Emission energy from the ground state ($k = 0$) as a function
of time (left) and the corresponding photoluminescence intensity
(right). The color code goes from black, no emission, to red, in-
tense emission, saturating in a black central region. (b) Spectral
line shapes extracted from (a). (c) In blue dots, average conden-
sate population n_0 (normalized photoluminescence intensity); in
purple squares, linewidth κ_0 (meV) of the emission peak, limited
by the spectral resolution of ~0.1 meV; in brown rhombus,
degree of linear polarization D_l. Times for coherence buildup
(t_1), maximum population (t_2), and coherence (t_3) are marked
with dashed lines. Inset: Polarization polar plot at $t = t_3$ with
maximum coherence for the present case (I) and for a second
point in the sample (II).

pation. Note that the blueshift is always much smaller
(<1 meV) than the Rabi splitting, so that the system
remains in strong coupling. As the reservoir depletes
with time, the overall population and the blueshift mono-
tonically decrease, while n_0 first increases and then de-
creases. The coherence imprinted by the laser pulse and its
original polarization is lost during this efficient cascade of
decays, populating the ground state with initially uncorre-
lated polaritons. This is clear from the linear polarization
D_l [brown rhombus in Fig. 1(c)] that takes some time to
build up after $n_0 \approx 1$. Past this particular time (correspond-
ing to $t_1 = 61$ ps in the figures), the system is above
threshold with a condensed fraction and a phase locking
of the spin-up and spin-down condensates. Stimulated
scattering into the ground state becomes the dominating
process, and the population n_0 grows up to a maximum
[with $\max(n_0) \approx 25$ at $t_2 = 118$ ps]. However, the coher-
ence reaches its maximum $\max(D_l) = 0.75$ at a later time
$t_3 = 140$ ps with a proper dynamics that does not follow

instantaneously that of n_0: D_l decays for another 150 ps at a different rate than that of the population. D_l is represented as a function of n_0 in Fig. 2(a) and compared with two other cases in order to make evident the existence of an hysteresis loop. As the excitation power is decreased, not only n_0 and D_l decrease, but the hysteresis also gradually disappears.

The linewidth of the ground-state emission is also dramatically affected by the condensation. In the simplest picture of a single mode with an effective pumping rate from all of the other states $W_0^{out} = \sum_k P_{k0}(1 + n_k)$ (n_k is the population of the kth state) and a radiative decay rate γ_0 at $k = 0$, the linewidth can be approximated by $\kappa_0 = (W_0^{out} + \gamma_0)/(1 + n_0)$. This expression is enough to understand qualitatively the linewidth dynamics. As shown in Fig. 1(c) (purple squares), κ_0 drops dramatically at the phase transition due to the exponential growth of n_0. Close to the maximum population, the linewidth reaches the limiting value of our spectral resolution (0.1 meV). Note that κ_0 not only depends on n_0 but is also affected (broadened) by the populations of the levels feeding the ground state, which are enhanced before the transition takes place. The steady state value of $\kappa_0 \rightarrow 0.9$ meV ($t > 300$ ps) corresponds to the linewidth of the bare ground-state polaritons γ_0. This results in another hysteresis shown in Fig. 2(c). Although polaritons, being interacting bosons, also suffer screening due to Coulomb interaction, this

effect is significant only at extremely high polariton densities [25]. This regime is never reached in our experiment. Kasprzak *et al.* [3] observed under cw excitation an increase in the linewidth [dashed green line in Fig. 2(c)] and attributed it to polariton-polariton interaction. However, we find that the ground-state population is too small to produce this effect (the particle number should be 3 orders of magnitude higher). The reason for such a significant increase of the linewidth is more likely to be found in the high number of reservoir particles, much higher than n_0 in the case of cw experiments. With our time-dependent excitation, excluding the first few tenths of a picosecond, the amount of particles in the reservoir is significantly smaller than that at the bottom of the polariton dispersion, reducing drastically this extra decoherence effect.

Our experiments on polariton coherence formation are supported by a simple two-level model [sketched in the inset in Fig. 3(a)] that links together the dynamics of the coherence degree with the population and the linear polarization. We work under the assumption—supported by the observation—that both spin components evolve similarly following this dynamics. We proceed in the spirit of the evaporative cooling description [26] that has been used before in models including polariton-polariton and photon-polariton scattering [25,27]. A reservoir, state 1, is populated in an incoherent way from higher levels, which we describe with an effective time-dependent rate $P_1(t)$ which has a Gaussian profile in time, reminiscent of the excitation of the laser at very high energy, with temporal effective width Δt_{pulse}. These particles are scattered incoherently into the ground state, level 0, at a different rate P_{10}. Both levels lose polaritons with decay rates γ_0 and γ_1, respectively. We also include the inverse process of promoting polaritons up the branch at some small rate γ_{01}.
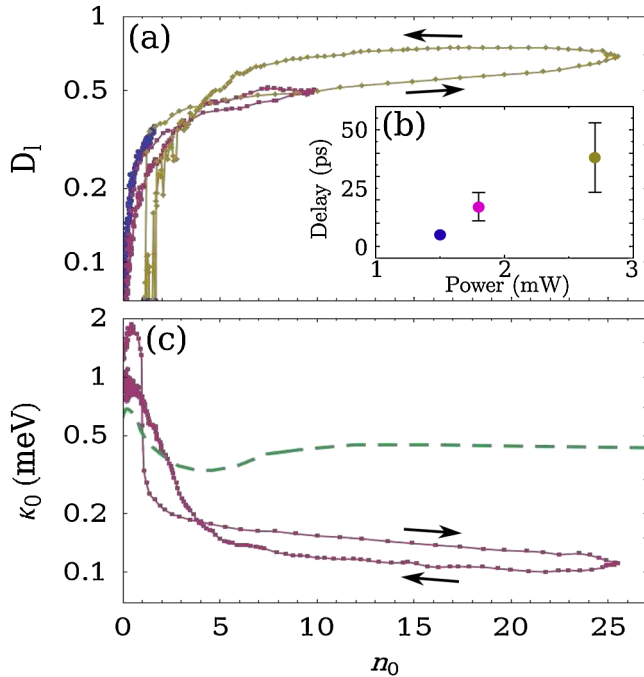

FIG. 2 (color online). Hysteresis in D_l (a) and κ_0 (c) as a function of n_0, with time running in the sense of the arrows. (a) Three experiments are shown with increasing excitation powers (the one under study in brown rhombus). (b) Growth with power of the delay between maximum population and coherence for these three cases. The linewidth of Ref. [3], under cw excitation, is given in (c) (dashed green line) for comparison.
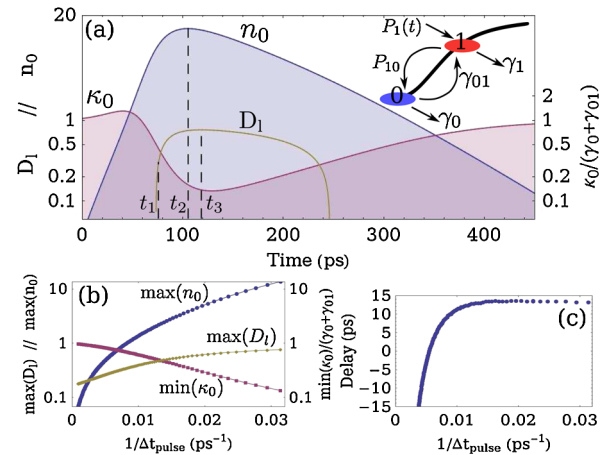

FIG. 3 (color online). (a) Theoretical results: n_0 (blue line), D_l (brown line), and κ_0 (purple line), as a function of time (rescaled to picoseconds for comparison). In (b), the maximum $max(n_0)$, $max(D_l)$, and minimum $min(\kappa_0)$ values reached in the simulations as the effective pulse narrows (with increasing $1/\Delta t_{pulse}$) down to the case in (a). The delay $t_3 - t_2$ between $max(n_0)$ and $max(D_l)$ is plotted in (c).

This dynamics is described with Lindblad terms in a master equation of the ground-state/reservoir system. This leads to rate equations for the time-dependent distributions of particles, which are solved numerically to compute the observables of interest (n_0, $g^{(2)}$, D_l, etc.). The linewidth is obtained from $\kappa_0 \approx [\gamma_{01}(1 + n_1) + \gamma_0]/(1 + n_0)$. In this model, the coherence builds up spontaneously, while other works [28] require a seed (such as an initial coherent state) in order to investigate the dynamics of coherence. The results, plotted in Fig. 3(a) with the same color code, are qualitatively similar to the experimental data in Fig. 1(c). With no need for more levels, we also reproduce the existence of a delay between maximum coherence and population. We find that when the effective pulse $P_1(t)$ gets sharper in time (small $1/\Delta t_{\text{pulse}}$), not only are $\max(n_0)$ and $\max(D_l)$ larger, but also the delay between them increases, as can be seen in Figs. 3(b) and 3(c). The delay can even become negative when the pulse is too flat. The origin and sign of the delay can be explained as follows: For a sharp and strong pulse, the ground-state population n_0 rises so quickly that coherence formation cannot simultaneously build up (through stimulated interaction with the upper level) and settles to its own, intrinsic dynamics instead (the delay becomes independent of the pulse duration as this one gets narrower). With a flat pulse, on the other hand, n_0 grows slowly and weakly, giving time to the condensate coherence to form together with it, possibly overtaking the dynamics for very long effective pulses and yielding a negative delay [Fig. 3(c)]. Increasing the inflow of particles (e.g., increasing P_{10}/γ_{01}) also has a similar effect of enhancing the coherence and its rising time. On the other hand, the total intensity of the pulse is not determining the delay. In the experiment, a more intense pulse also results in a sharper profile for the effective excitation, given that the chain of deexcitations towards level 1 is more efficient, thanks to the density dependence of the exciton-exciton scattering [29].

Finally, although our simple model does not lead to a quantitative agreement with the experiments (time has been rescaled for a better comparison), it is of a fundamental character, since it contains the minimum number of elements to reproduce BEC formation and links together its essential features (population, coherence, linewidth, and polarization). The model should include more levels in the deexcitation chain towards the ground state to reach to a quantitative agreement, not bringing, however, any essential new features into the description (as we have checked but which we do not discuss here).

In conclusion, we report the experimental observation of the dynamics of a polariton condensate, created under a nonresonant, circularly polarized pulse, and the study of its coherence buildup and decay. We track the order parameter of the transition through the degree of linear polarization that spontaneously builds up. This occurs when the average population of the ground state exceeds one and is accompanied by an abrupt decrease in the emission linewidth. The maximum degree of coherence that is achieved does not coincide in time with the maximum population, evidencing that the coherence of the condensate has its own particular dynamics. The pulsed excitation regime is a worthy tool revealing neatly the interplay of all of the relevant quantities of polariton condensates and displaying the mechanisms of the formation and decay of a BEC. We support our claims with a simple theoretical model.

*Present address: Laboratoire Kastler Brossel, Université Pierre et Marie Curie, Ecole Normale Supérieure et CNRS, UPMC Case 74, 75252 Paris Cedex 05, France.

[1] C. Weisbuch et al., Phys. Rev. Lett. **69**, 3314 (1992).
[2] A. Kavokin et al., Microcavities (Oxford University, New York, 2007).
[3] J. Kasprzak et al., Nature (London) **443**, 409 (2006).
[4] R. Balili et al., Science **316**, 1007 (2007).
[5] S. Christopoulos et al., Phys. Rev. Lett. **98**, 126405 (2007).
[6] J. J. Baumberg et al., Phys. Rev. Lett. **101**, 136409 (2008).
[7] D. Bajoni et al., Phys. Rev. Lett. **100**, 047401 (2008).
[8] M. Anderson et al., Science **269**, 198 (1995).
[9] K. B. Davis et al., Phys. Rev. Lett. **75**, 3969 (1995).
[10] H. Deng et al., Phys. Rev. Lett. **99**, 126403 (2007).
[11] J. Kasprzak et al., Phys. Rev. Lett. **100**, 067402 (2008).
[12] A. P. D. Love et al., Phys. Rev. Lett. **101**, 067404 (2008).
[13] A. Amo et al., Nature (London) **457**, 291 (2009).
[14] After the first submission of this text, more experiments on polariton BEC dynamics were reported by G. Nardin et al., arXiv:0905.2337.
[15] D. Read et al., arXiv:0807.0980.
[16] F. P. Laussy et al., Phys. Rev. B **73**, 035315 (2006).
[17] I. A. Shelykh et al., Phys. Rev. Lett. **97**, 066402 (2006).
[18] G. Lachs, Phys. Rev. **138**, B1012 (1965).
[19] M. D. Martin et al., Phys. Rev. Lett. **89**, 077402 (2002).
[20] Ł. Kłopotowski et al., Solid State Commun. **139**, 511 (2006).
[21] T. D. Doan et al., Phys. Rev. B **72**, 085301 (2005).
[22] N. Peyghambarian et al., Phys. Rev. Lett. **53**, 2433 (1984).
[23] S. Schmitt-Rink, C. Ell, and H. Haug, Phys. Rev. B **33**, 1183 (1986).
[24] C. Ciuti et al., Phys. Rev. B **62**, R4825 (2000).
[25] D. Porras and C. Tejedor, Phys. Rev. B **67**, 161310(R) (2003).
[26] M. Holland et al., Phys. Rev. A **54**, R1757 (1996).
[27] F. P. Laussy et al., Phys. Rev. Lett. **93**, 016402 (2004).
[28] Y. G. Rubo et al., Phys. Rev. Lett. **91**, 156403 (2003).
[29] L. Muñoz et al., Phys. Rev. B **51**, 4247 (1995).